Multifactor asset pricing with a large number of

observable risk factors and unobservable common

and group-specific factors

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Abstract

This paper analyzes multifactor models in the presence of a large number of po-

tential observable risk factors and unobservable common and group-specific pervasive

factors. We show how relevant observable factors can be found from a large given set

and how to determine the number of common and group-specific unobservable factors.

The method allows consistent estimation of the beta coefficients in the presence of

correlations between the observable and unobservable factors. The theory and method

are applied to the study of asset returns for A-shares/B-shares traded on the Shanghai

and Shenzhen stock exchanges, and to the study of risk prices in the cross section of

returns.

Key words: factor models, panel data analysis, penalized method, LASSO, SCAD,

heterogenous coefficients

JEL Clarification codes: C23, C52, G12

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